



Chemical evolution in L-GALAXIES:

implementation & comparison to obs

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GCE analytics

GCE implementation

To model GCE, we need to know...

1) How many stars of mass M die at time t

$$\text{IMF} \bullet \text{SFR}(t-T_M) = \text{death rate at time } t$$

2) How much metal they eject at time t

$$M_Z = \text{Metal mass ejected by star of mass } M$$

Therefore:

$$\text{IMF} \bullet \text{SFR}(t-T_M) \bullet M_Z = \text{Metal mass ejected by star of mass } M \text{ at time } t$$

The GCE equation

$$e_Z(t) = \int_{M_L}^{M_U} M_Z(M, Z_0) \psi(t - \tau_M) \phi(M) dM$$

↑ Metals ↑ SFR ↑ IMF

$e_Z(t)$ = The rate of ejection of metals from a simple stellar population (SSP)

$$M_Z = y_Z(M, Z_0) + Z_0 \cdot (M - M_r)$$

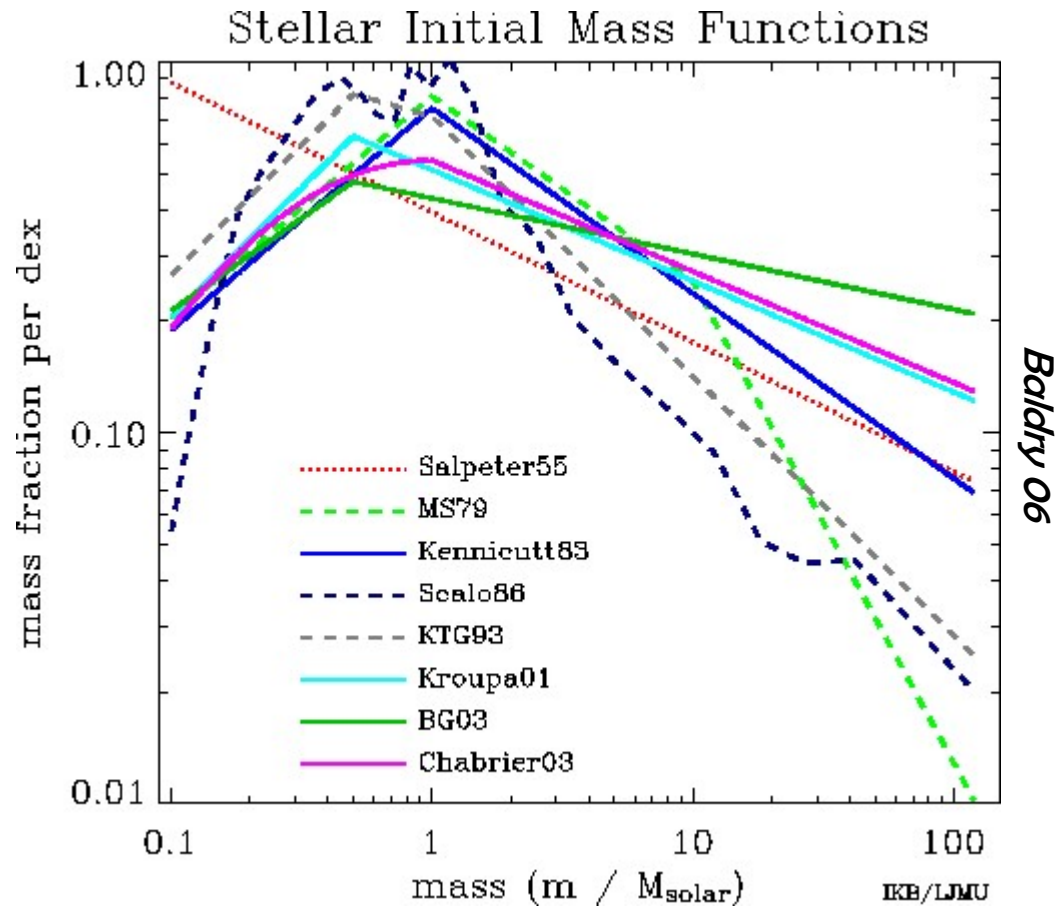
= The mass of metals ejected by one star of initial mass M , initial metallicity Z_0 and remnant mass M_r .

$\psi(t - \tau_M)$ = The star-formation rate (SFR) at a time τ_M in the past

$\phi(M)$ = The stellar initial mass function (IMF)

The IMF

$$e_Z(t) = \int_{M_L}^{M_U} M_Z(M, Z_0) \psi(t - \tau_M) \phi(M) dM$$



The IMF tells us how many stars of mass M there are.

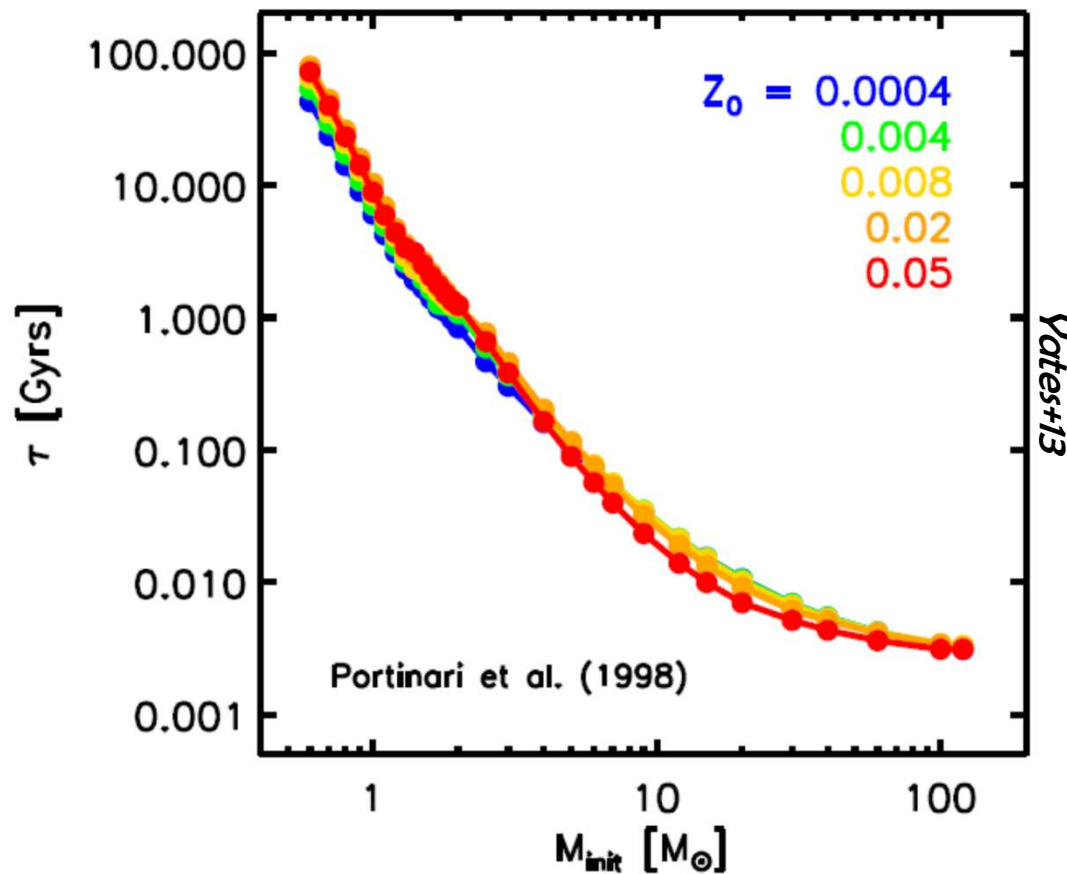
Different IMFs give different GCE results. e.g. more high-mass stars means more alpha elements...

Currently in L-GALAXIES, we assume a Chabrier 03 IMF (fixed in time and space), with $M_L = 0.1 M_{\text{sun}}$ and $M_U = 120 M_{\text{sun}}$:

$$\phi(M) = \begin{cases} A_\phi M^{-1} e^{-(\log M - \log M_c)^2 / 2\sigma^2} & \text{if } M \leq 1M_\odot \\ B_\phi M^{-2.3} & \text{if } M > 1M_\odot \end{cases}$$

Stellar lifetimes

$$e_z(t) = \int_{M_L}^{M_U} M_Z(M, Z_0) \psi(t - \tau_M) \phi(M) dM$$



Simple, monotonic link between τ_M and M .

$(t - \tau_M)$ is therefore the birth time of a star of mass M exploding at time t .

Currently in L-GALAXIES, we assume the weakly Z -dependent lifetimes of *Portinari+98*.

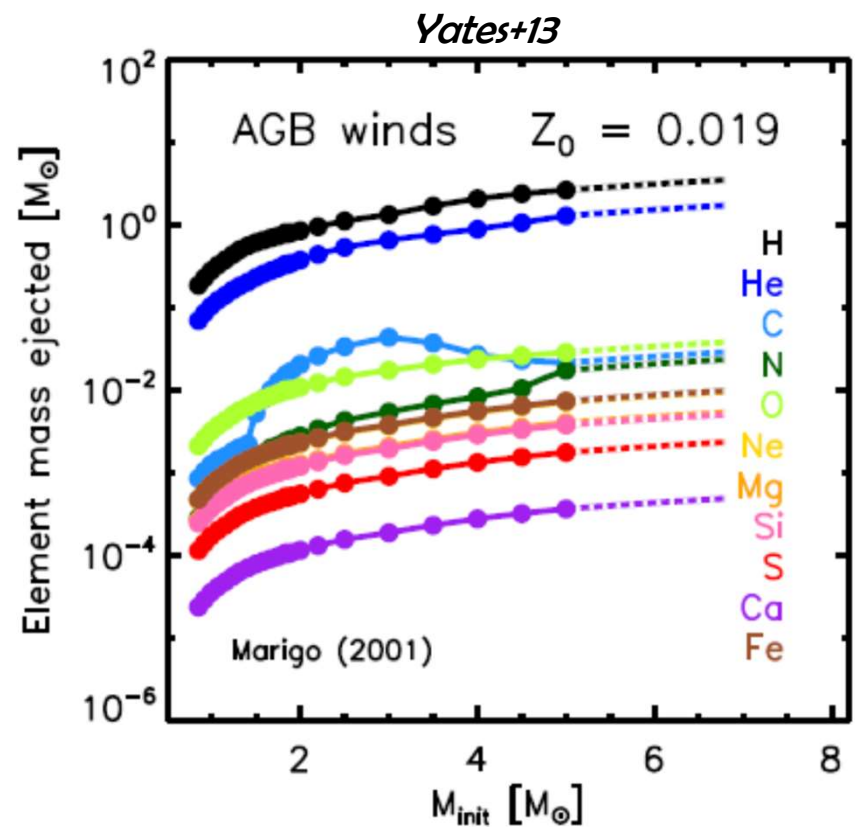
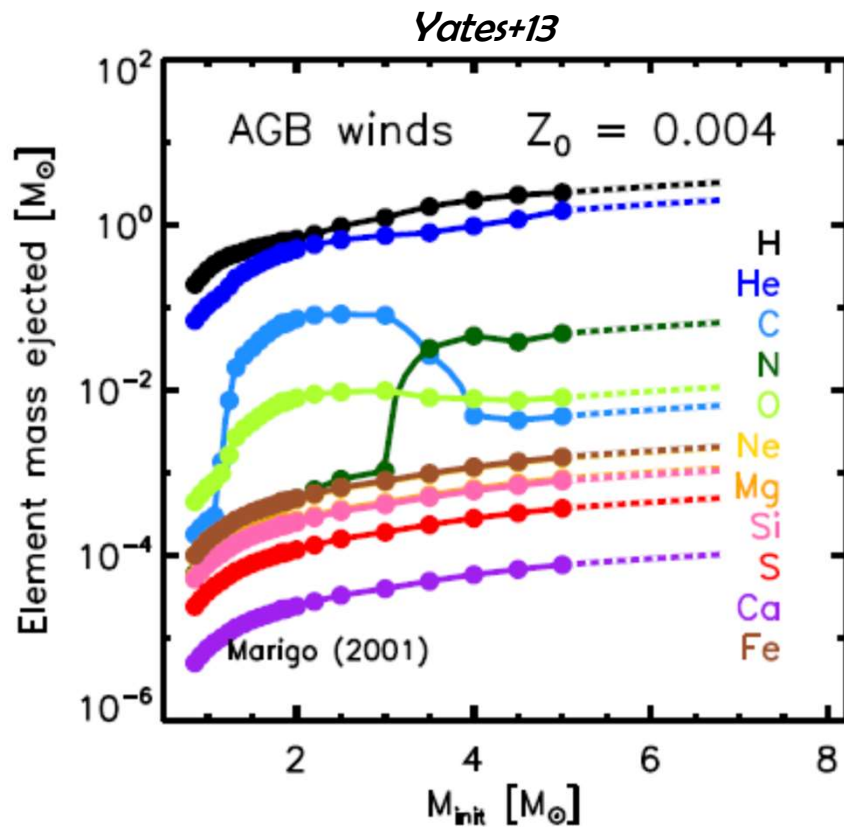
AGB winds

$$e_Z(t) = \int_{M_L}^{M_U} M_Z(M, Z_0) \psi(t - \tau_M) \phi(M) dM$$

Intermediate-mass stars ($0.85 - 7 M_{\text{sun}}$) eject their outer layers during the thermally-pulsating asymptotic giant branch (AGB) phase.

Currently in L-GALAXIES, we use the AGB wind yields of *Marigo 01*.

(We approximate that the winds eject at the end of the stars' lives)



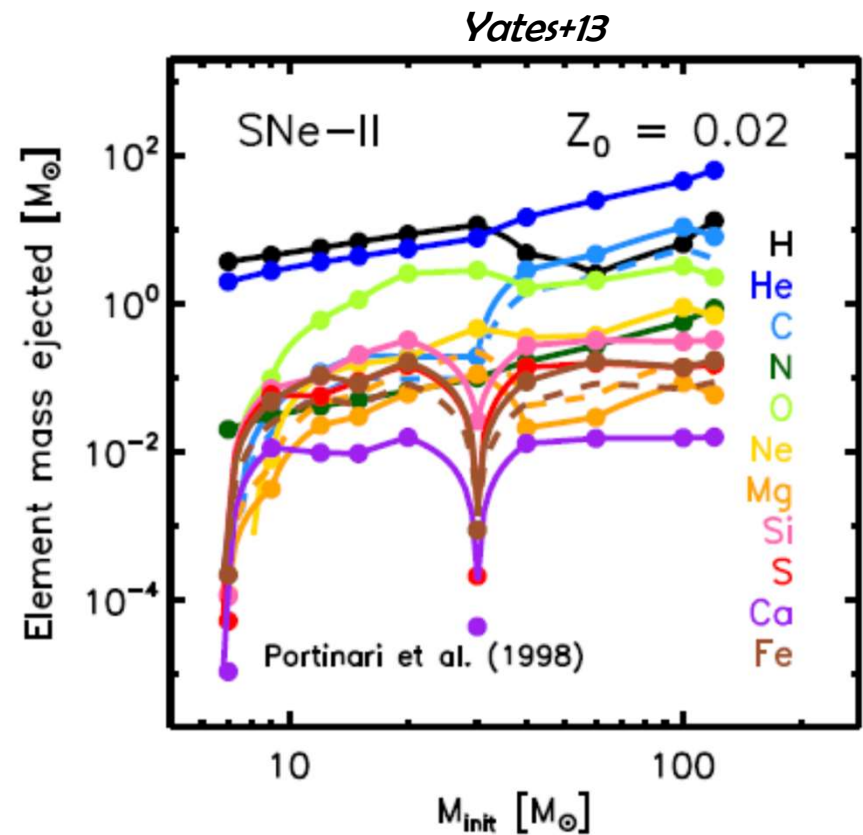
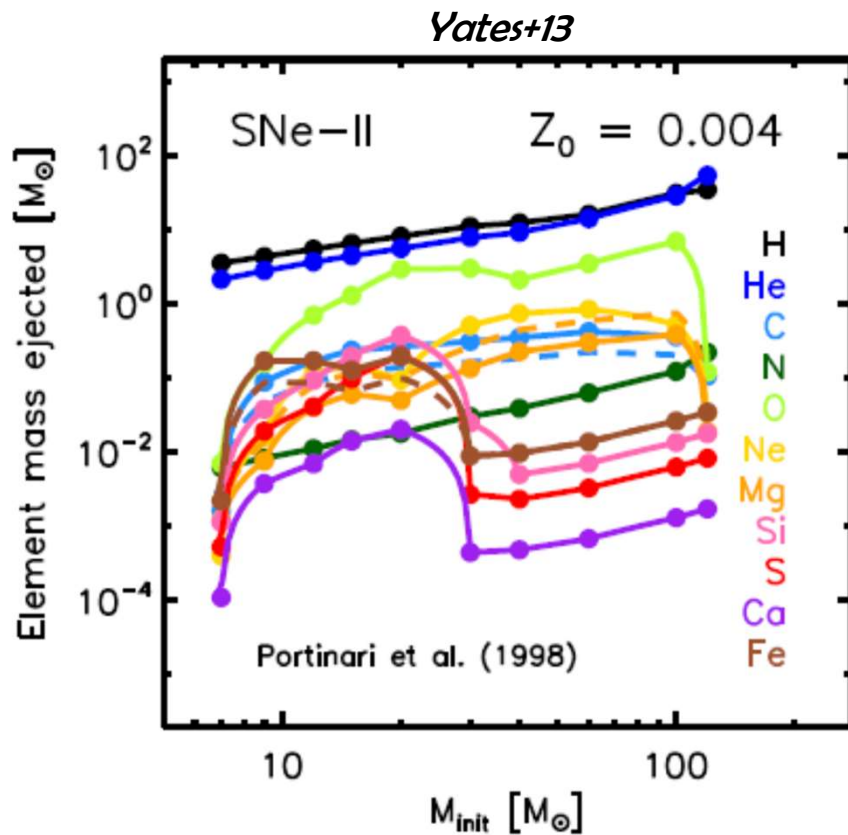
SNe-II

$$e_Z(t) = \int_{M_L}^{M_U} M_Z(M, Z_0) \psi(t - \tau_M) \phi(M) dM$$

Massive stars ($>7 M_{\text{sun}}$) are assumed to explode mainly as type II core-collapse supernovæ (SN-II). These eject predominantly alpha elements (and H & He).

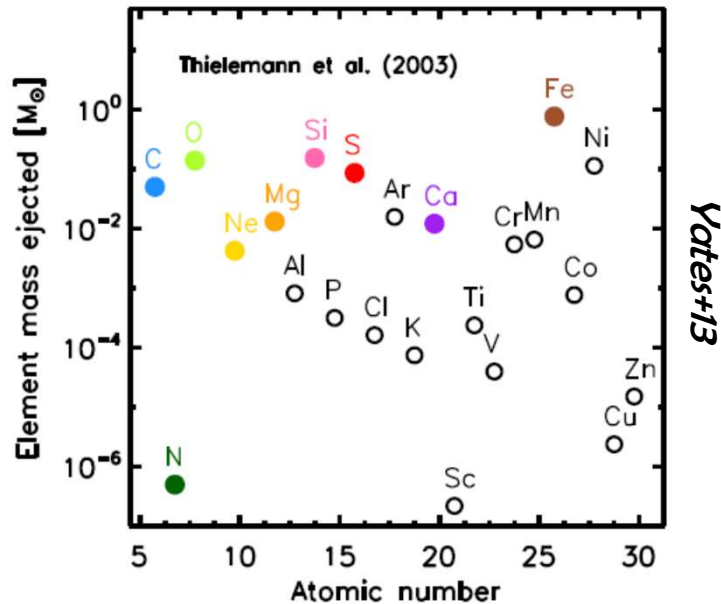
Currently in L-GALAXIES, we consider the SN-II yields of *Portinari+98*.

(Note the strong mass-dependence for the *Portinari+98* yields)



SNe-Ia

$$e_Z(t) = \int_{M_L}^{M_U} M_Z(M, Z_0) \psi(t - \tau_M) \phi(M) dM$$



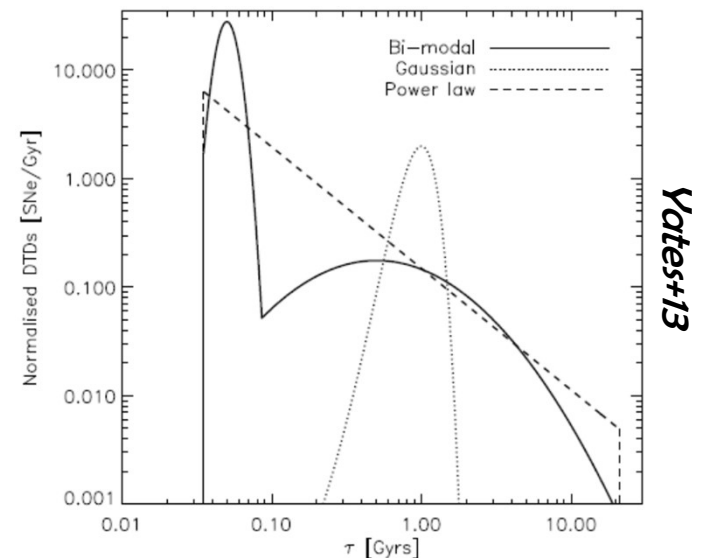
Some binary systems (2.8%) with total mass $3 - 16 M_{\text{sun}}$ (companion star mass $0.85 - 8 M_{\text{sun}}$) can explode as type Ia supernovae. These eject mainly Fe.

Currently in L-GALAXIES, we use the SN-Ia yields of Thielemann+03.

We allow some binary systems to blow AGB winds *and* explode as SNe-Ia.

The lifetimes of these binary systems are determined empirically, via a SN-Ia delay-time distribution (DTD).

Currently in L-GALAXIES, we include four different DTDs, with $\tau_{\text{min}} = \tau_{8M_{\text{sun}}} = 35 \text{ Myr}$ and $\tau_{\text{max}} = \tau_{0.85M_{\text{sun}}} = 21 \text{ Gyr}$.



The detailed GCE equation

$$\begin{aligned}
 e_Z(t) = & \int_{0.85M_\odot}^{7M_\odot} M_Z^{\text{AGB}}(M, Z_0) \psi(t - \tau_M) \phi(M) dM && \longleftarrow \text{AGB winds} \\
 & + A' k \int_{\tau_{8M_\odot}}^{\tau_{0.85M_\odot}} M_Z^{\text{Ia}} \psi(t - \tau) \text{DTD}(\tau) d\tau && \longleftarrow \text{SNe-Ia} \\
 & + (1 - A) \int_{7M_\odot}^{16M_\odot} M_Z^{\text{II}}(M, Z_0) \psi(t - \tau_M) \phi(M) dM && \longleftarrow \text{SNe-II} \\
 & + \int_{16M_\odot}^{M_{\text{max}}} M_Z^{\text{II}}(M, Z_0) \psi(t - \tau_M) \phi(M) dM . && \longleftarrow \text{SNe-II}
 \end{aligned}$$

$A = 0.028$ = Fraction of stellar systems in range 3 – 16 M_{sun} that are SN-Ia progenitor binaries.

$f_{3-16} = 0.0385$ = Fraction of *all* stellar systems that are in range 3 – 16 M_{sun} .

$A' = A \cdot f_{3-16} = 0.0011$ = Fraction of *all* stellar systems that are SN-Ia progenitor binaries.

$k = \int_{M_{\text{min}}}^{M_{\text{max}}} \phi(M) dM = 1.4772$ = Number of stellar objects in a 1 M_{sun} SSP.

These parameters are all dependent on the IMF's shape & mass range.

In L-GALAXIES, A is tuned to the [Fe/H] distribution in the Milky Way stellar disc (Yates+13).

GCE coding

yields_read_tables.c

```
#include <stdio.h>
#include <stdlib.h>
#include <string.h>
#include <math.h>
#include <time.h>

#include "allvars.h"
#include "proto.h"

void read_yield_tables(void)
{
    //-----
    //READ LIFETIME MASS LIST:
    //-----
    FILE *fd1;
    char buf1[100];
    int il;
    float m1;
    static char *name1 = "stripped_interp_LifetimeMasses.txt";

    sprintf(buf1, "./YieldTables/%s", name1);

    if(!(fd1 = fopen(buf1, "r")))
    {
        printf("file '%s' not found.\n", buf1);
        exit(0);
    }

    for(il=0; il<LIFETIME_MASS_NUM; il++)
    {
        fscanf(fd1, "%f %s", &m1, &name1);
    }
}
```

Chabrier 03 IMF is coded here:
Chabrier_IMF().

read_yield_tables() is called
from *init.c*.

Reads yield tables and convolves them with the IMF.

Creates 2- or 3-dimensional arrays. e.g. *SNII TotalMetals[SNII_Z_NUM][SNII_MASS_NUM]*

yields_integrals.c

```
/*
 * yields_integrals.c
 *
 * Pre-calculates the normalised ejecta rates
 * Multiply by SFR from SFH bins (and interpo
 * true ejecta rates (done in recipe_yields.c
 *
 * Created on: 10.05.2012
 * Author: robyates
 */

#include <stdio.h>
#include <stdlib.h>
#include <string.h>
#include <math.h>
#include <time.h>

#include "allvars.h"
#include "proto.h"

#ifdef DETAILED_METALS_AND_MASS_RETURN

void integrate_yields()
{
    double previoustime, newtime, deltaT;
    int snap, step, i, mb;
    double timet;

    int Mi_lower, Mi_upper, Mi_lower_SNI, Mi
    int Zi_correc;
    int Mi_lower_AGP, Mi_upper_AGP, + lower 1

```

(Pre-)integrates the GCE equation, without model-dependent variables.

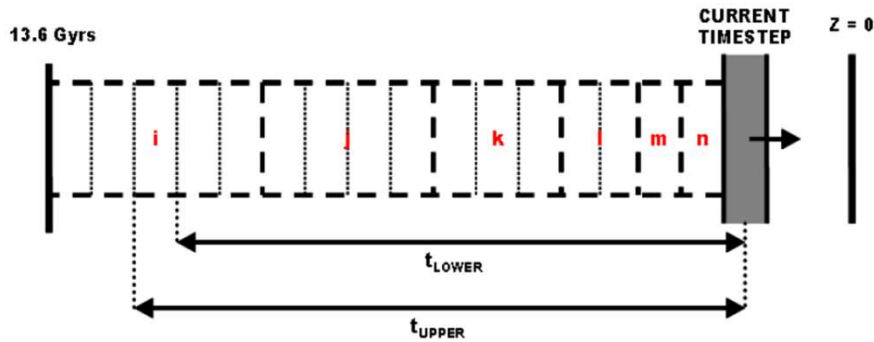
$$e_Z(t) = \psi(t - \tau) \left[\int_{M_L}^{M_U} M_Z(M, Z_0) \cdot \phi(M) dM \right]$$

The 'normalised' ejecta rate is calculated for N 'mini bins' in every SFH bin of every timestep, for 6 metallicities, and stored in 3D arrays (look-up tables).

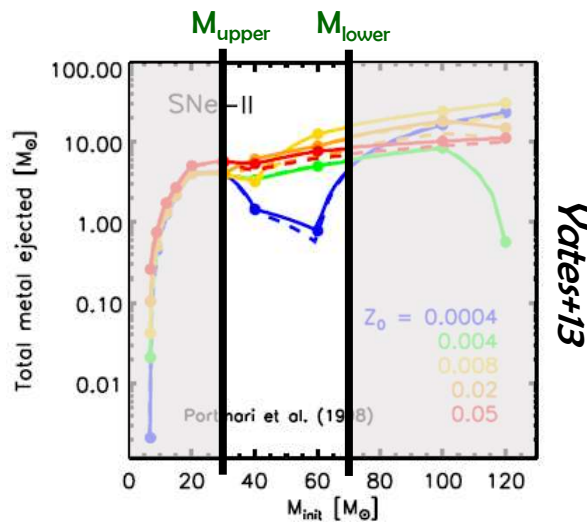
```
{ //Snapshots
{ //Timesteps
{ //SFH bins
{ //Mini bins (in-code sub-divisions of the SFH bins)
{ //Metallicities
    e.g. NormSNIIMetalEjecRate[step][SFHbin][Z]
}
}
}
}
}
```

init_integrated_yields() is called from *init.c*.

yields_integrals.c



1) A maximum (M_{lower}) and minimum (M_{upper}) mass of stars to die in the current timestep from each mini bin is calculated.

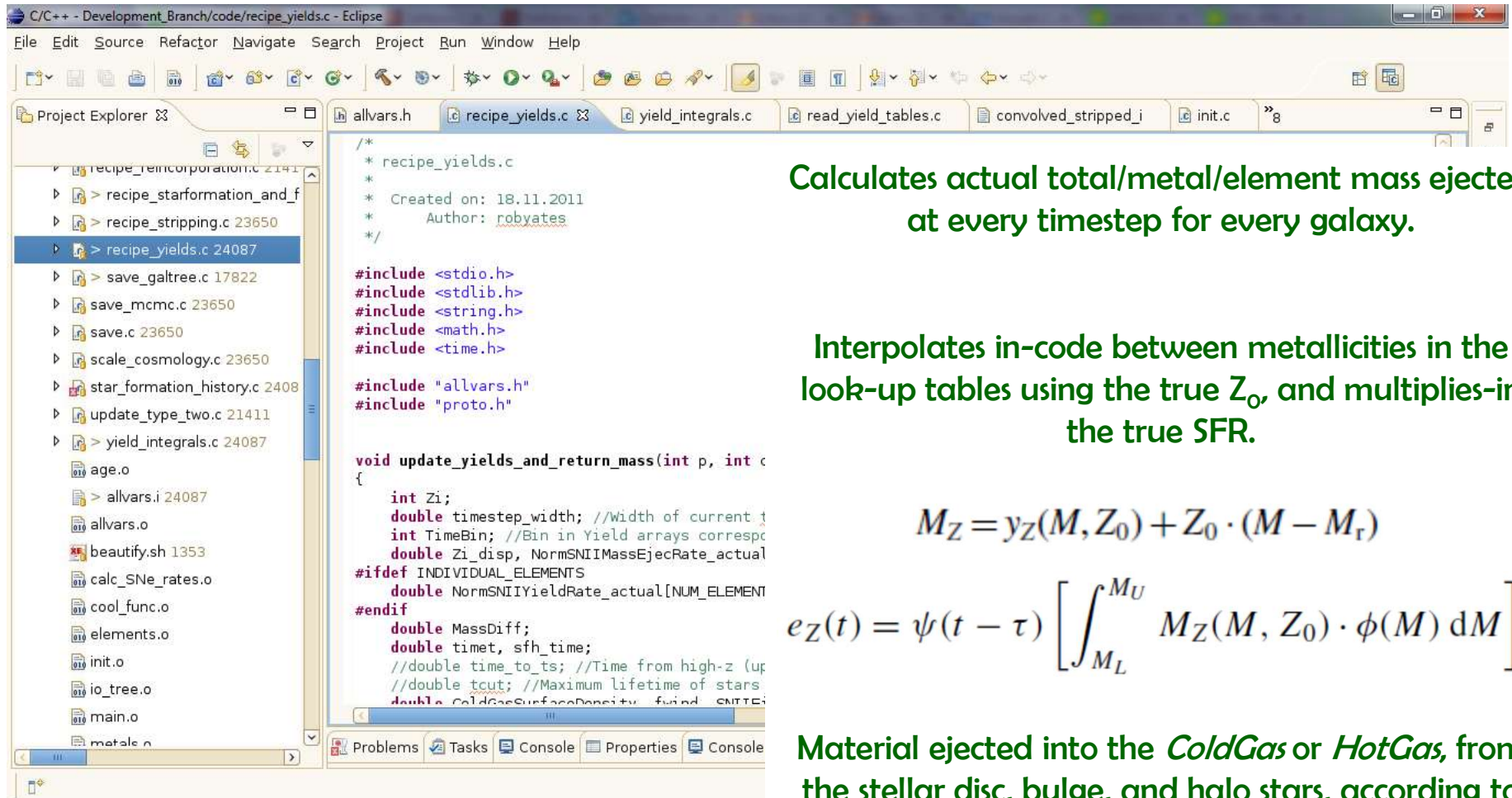


2) The total/metal/element mass ejected is integrated over numerically between M_{upper} and M_{lower} .

3) The many *if* statements in *yields_integrals.c* account for different limits when integrating across the finite-resolution yield tables. e.g. M_{upper} and M_{lower} will likely be *between* two masses in the yield table grid – sometimes even both between the *same* two masses.



model_yields.c



```
/*
 * recipe_yields.c
 * Created on: 18.11.2011
 * Author: robyates
 */

#include <stdio.h>
#include <stdlib.h>
#include <string.h>
#include <math.h>
#include <time.h>

#include "allvars.h"
#include "proto.h"

void update_yields_and_return_mass(int p, int c
{
    int Zi;
    double timestep_width; //width of current t
    int TimeBin; //Bin in Yield arrays correspo
    double Zi_disp, NormSNIIYieldRate_actual
#ifdef INDIVIDUAL_ELEMENTS
    double NormSNIIYieldRate_actual[NUM_ELEMENT
#endif
    double MassDiff;
    double timet, sfh_time;
    //double time_to_ts; //Time from high-z (up
    //double tcut; //Maximum lifetime of stars
    double ColdGasSurfaceDensity, fwind, SNII;
```

Calculates actual total/metal/element mass ejected at every timestep for every galaxy.

Interpolates in-code between metallicities in the look-up tables using the true Z_0 , and multiplies-in the true SFR.

$$M_Z = y_Z(M, Z_0) + Z_0 \cdot (M - M_r)$$

$$e_Z(t) = \psi(t - \tau) \left[\int_{M_L}^{M_U} M_Z(M, Z_0) \cdot \phi(M) dM \right]$$

Material ejected into the *ColdGas* or *HotGas*, from the stellar disc, bulge, and halo stars, according to the chosen GCE set-up

update_yields_and_return_mass() is called from *main.c*, after star formation, merging, and black hole growth.

GCE *makefile* options

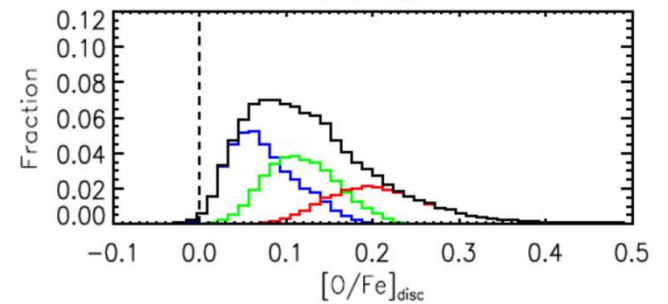
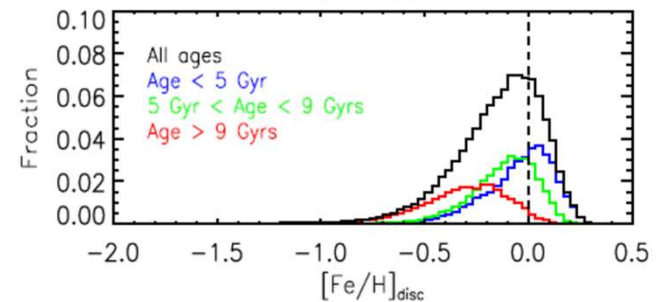
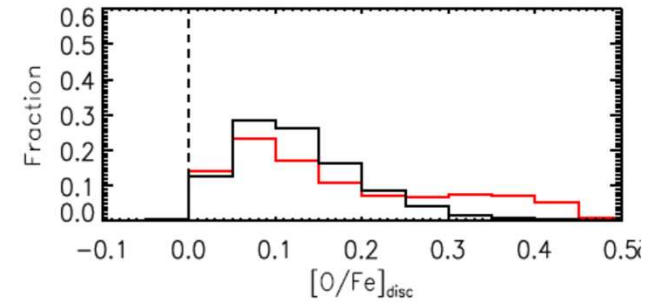
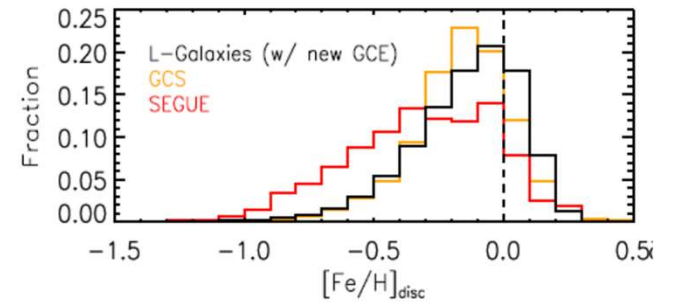
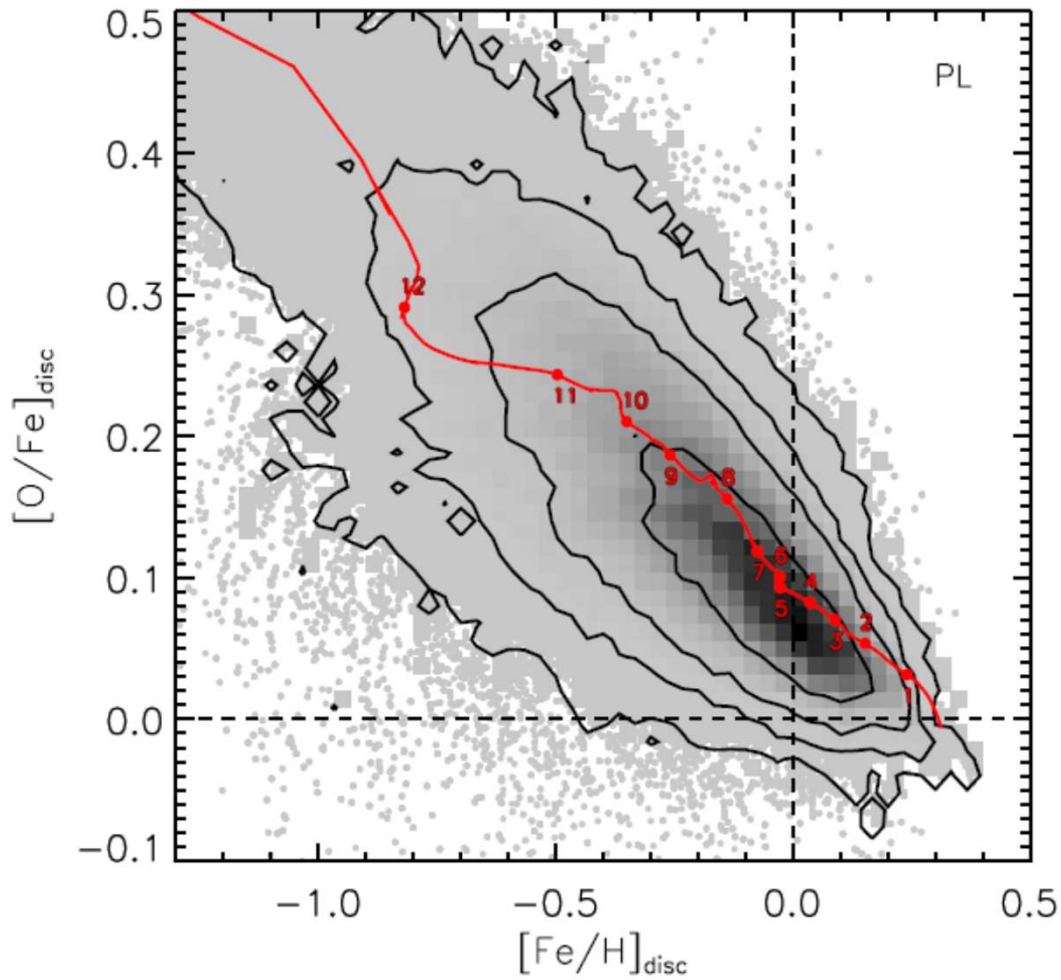
In *My_makefile_options* are the following GCE switches:

- OPT += -DFEEDBACK_COUPLED_WITH_MASS_RETURN: Switches on coupling between SN feedback and the chemical enrichment model.
- OPT += -DINDIVIDUAL_ELEMENTS: Switches on tracking of all 11 individual chemical elements.
- OPT += -DMAINELEMENTS: Switches on tracking of only 5 key chemical elements.
- OPT += -DMETALRICHWIND: Switches on galactic winds with a metallicity independent of that in the ISM.
- OPT += -DSNIATOHOT: Switches on direct enrichment of the CGM/ICM by SNe-Ia in the stellar disc.
- OPT += -DPORTINARI and -DCHIEFFI: Switch on the SN-II stellar yields of Portinari et al. (1998) or Chieffi & Limongi (2004).
- OPT += -DBIMODALDTD and -DGAUSSIANDTD and -DPOWERLAWDTD and -DRUITERDTD: Switch on one of the possible SN-Ia DTDs.
- OPT += -DINSTANTANEOUS_RECYCLE: Switches on instant return of metals at time of star formation, rather than at time stars die.

Past & future GCE projects

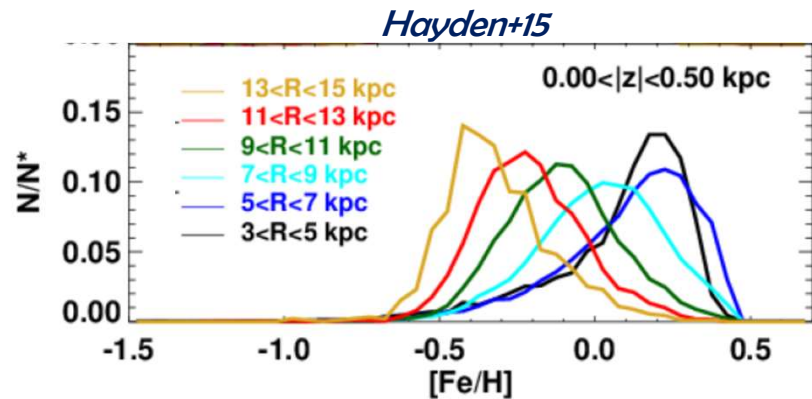
The Milky Way

$[\text{Fe}/\text{H}] - [\alpha/\text{Fe}]$ relation for MW disc stars
is obtainable

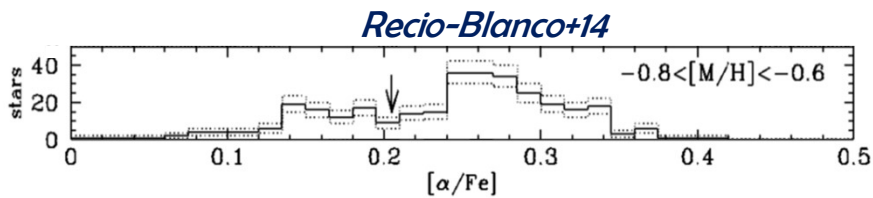


The Milky Way

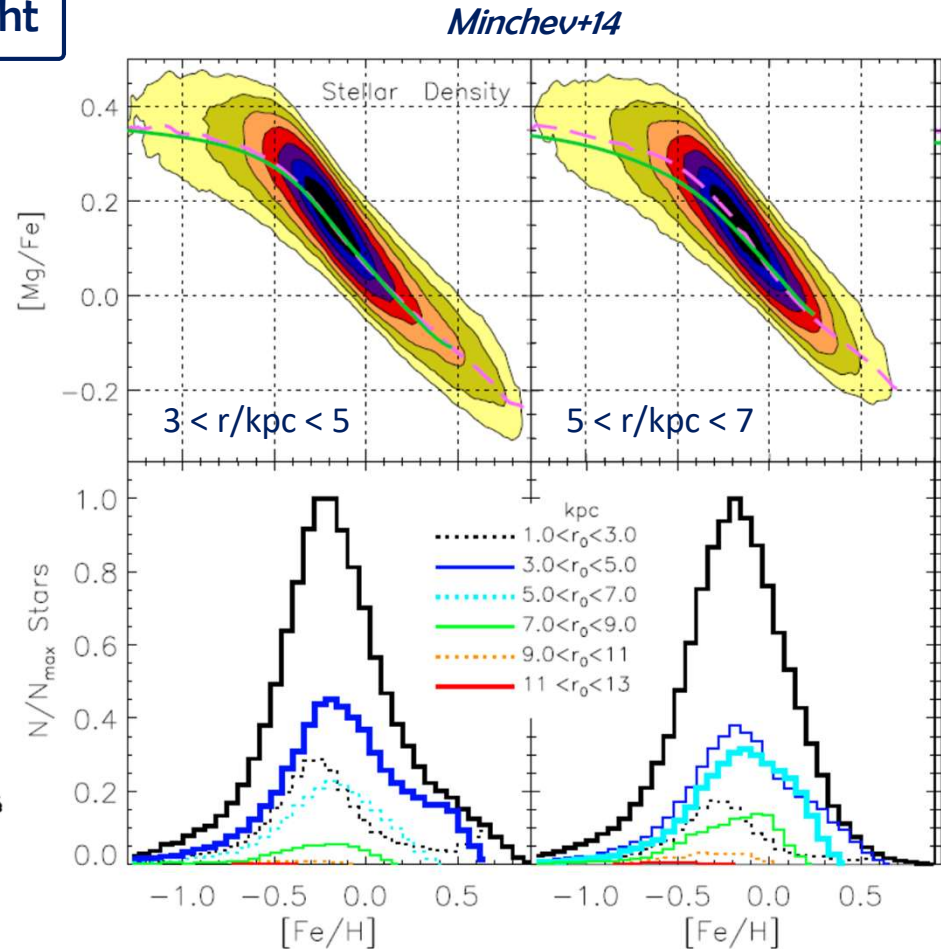
Chemical variations with radius and height



(Observations of ~70,000 red giants from the SDSS-APOGEE survey)



(Observations of ~1,000 FGK-type stars from the *Gaia*-ESO survey)

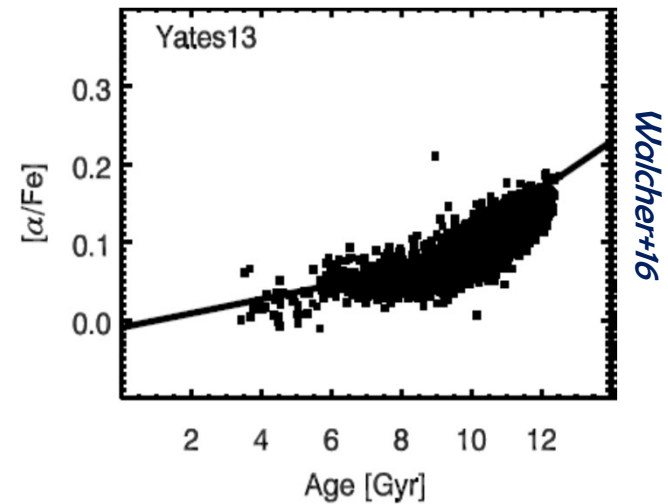
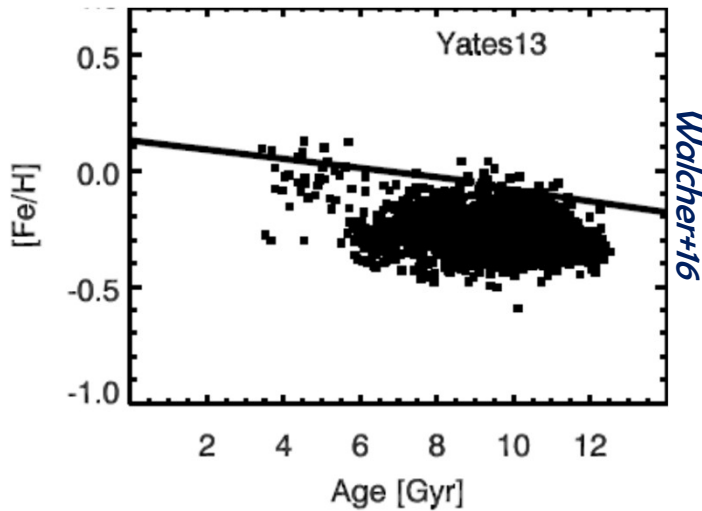
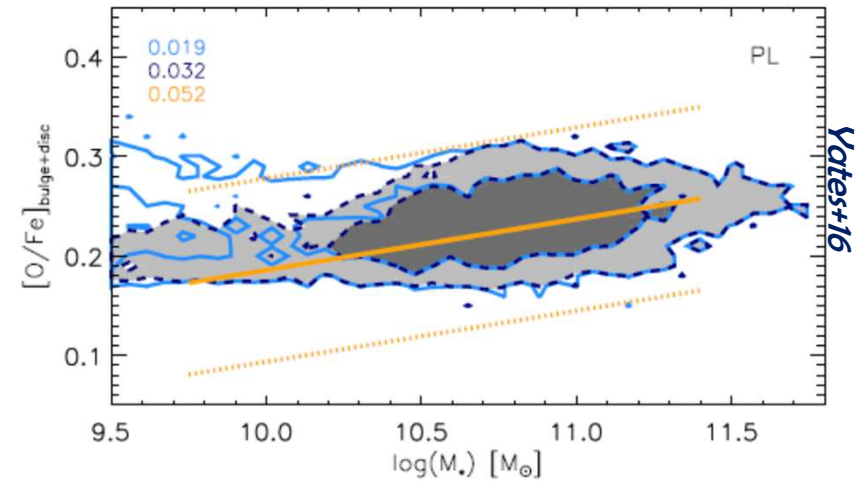
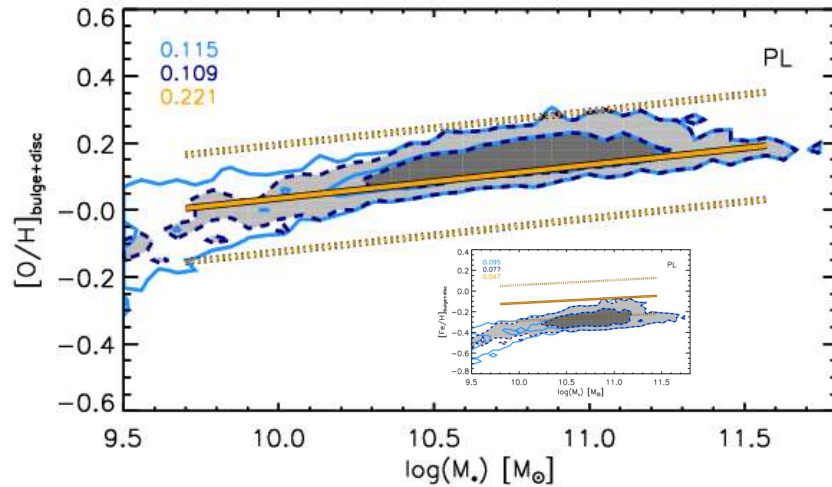


Is there a chemically-distinct thick disc?
(e.g. Bovy+12b; Schönrich & Binney 09)

The roles of metal mixing, radial migration, gas flows, mass-loaded outflows, etc, should be assessed

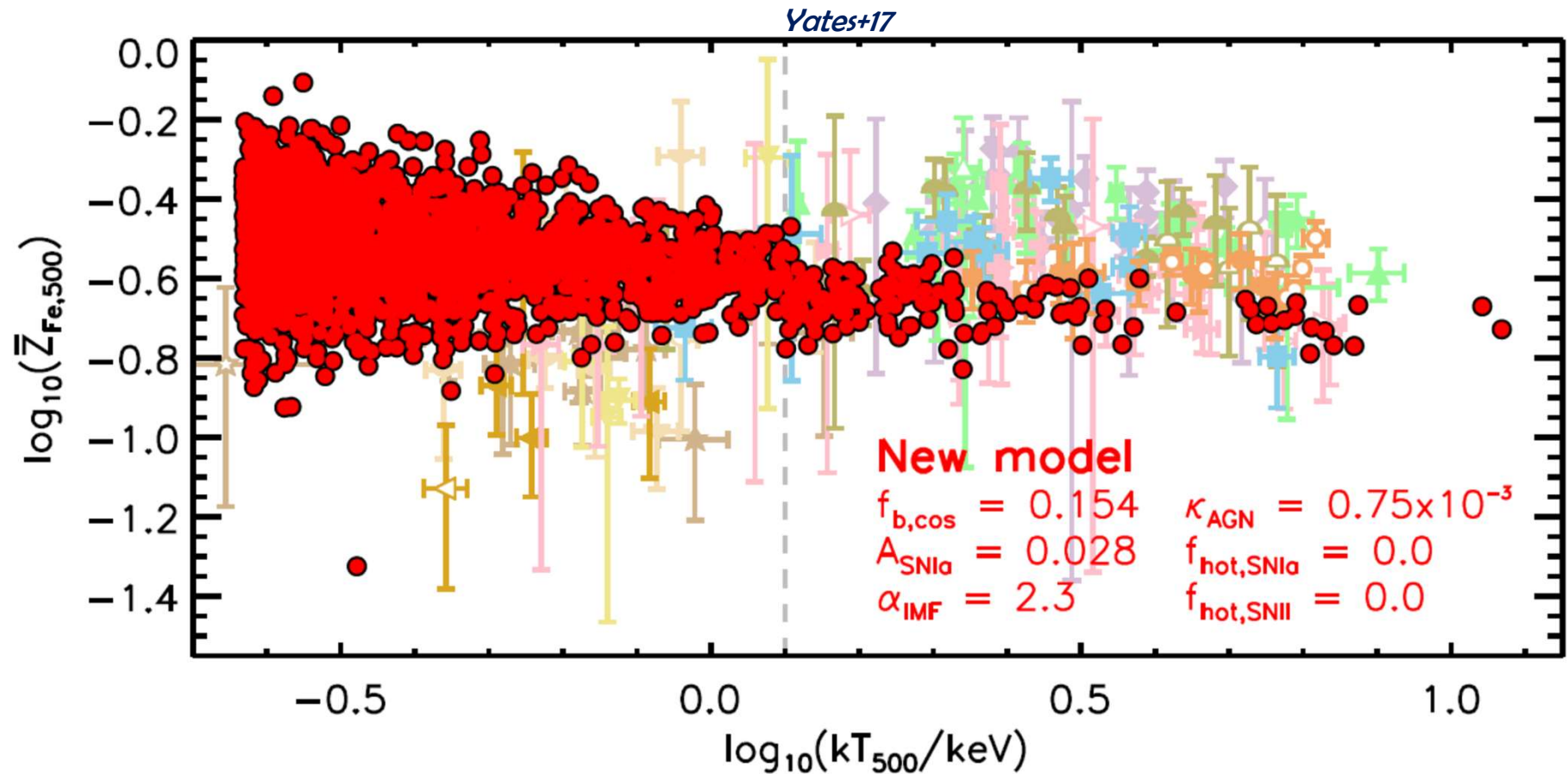
Early-type galaxies

Relations between key stellar population properties are simultaneously matched
age, mass, $[\text{Fe}/\text{H}]$ and $[\alpha/\text{Fe}]$



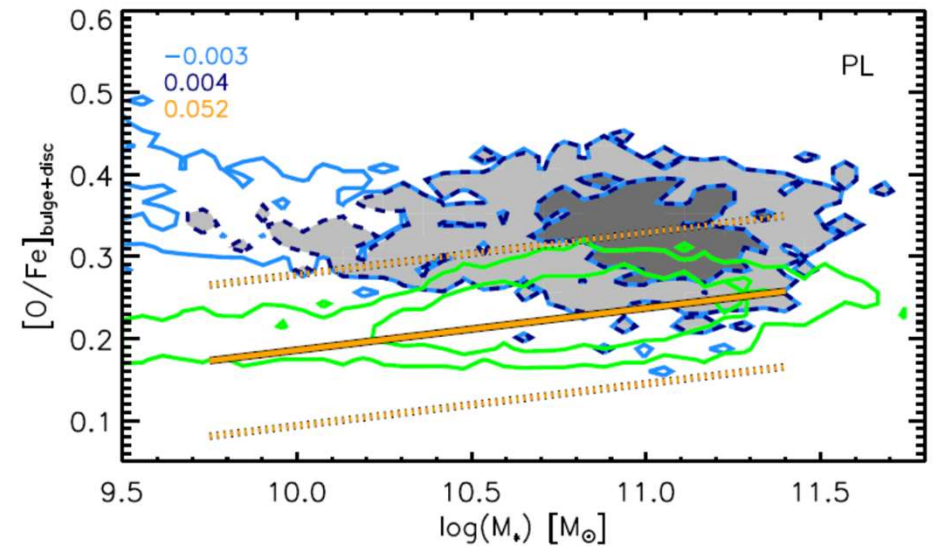
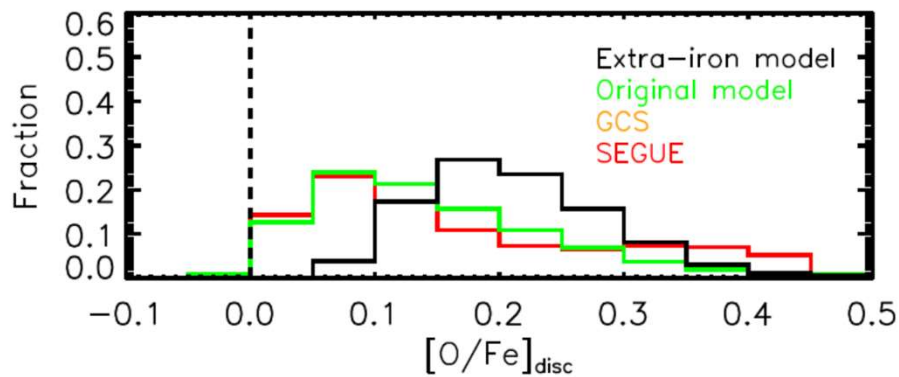
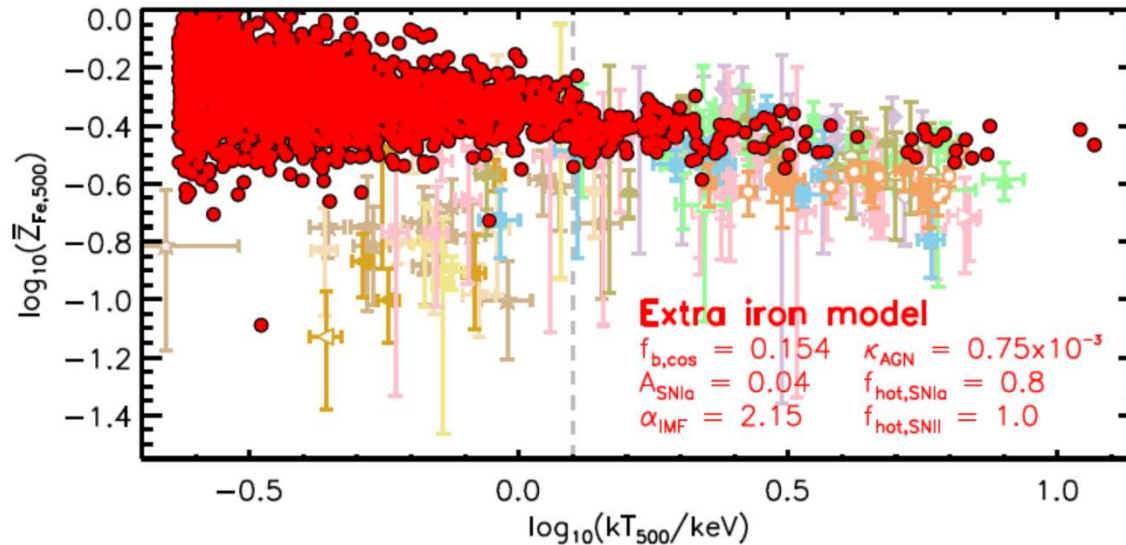
Intracluster medium

A highly-enriched ICM is now obtainable with improved infall/FB modelling and fairer comparisons to observations



Intracluster medium

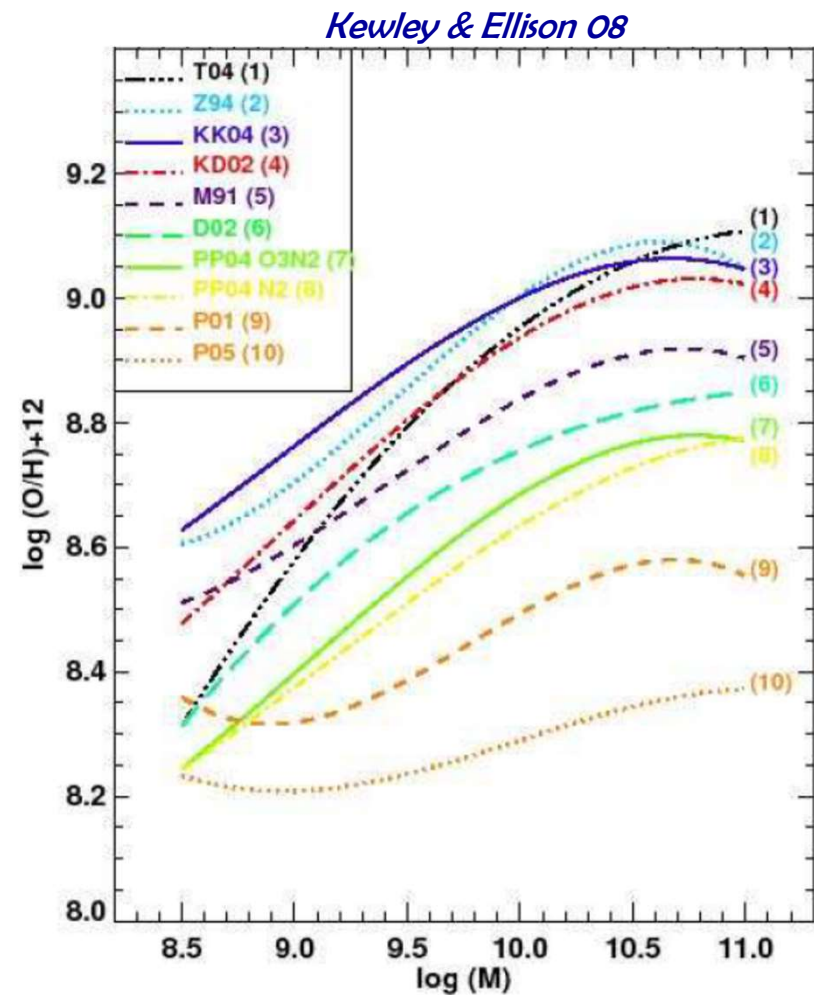
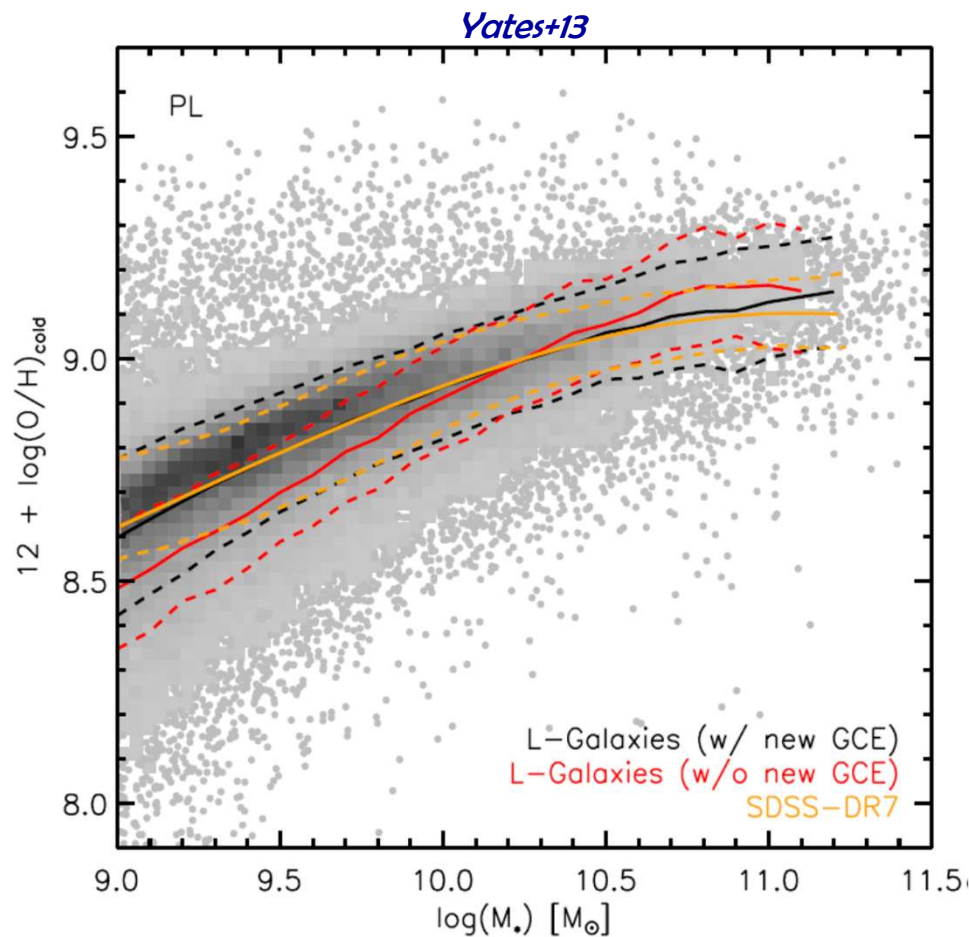
But we need to be careful not to destroy the consistency with other types of systems...



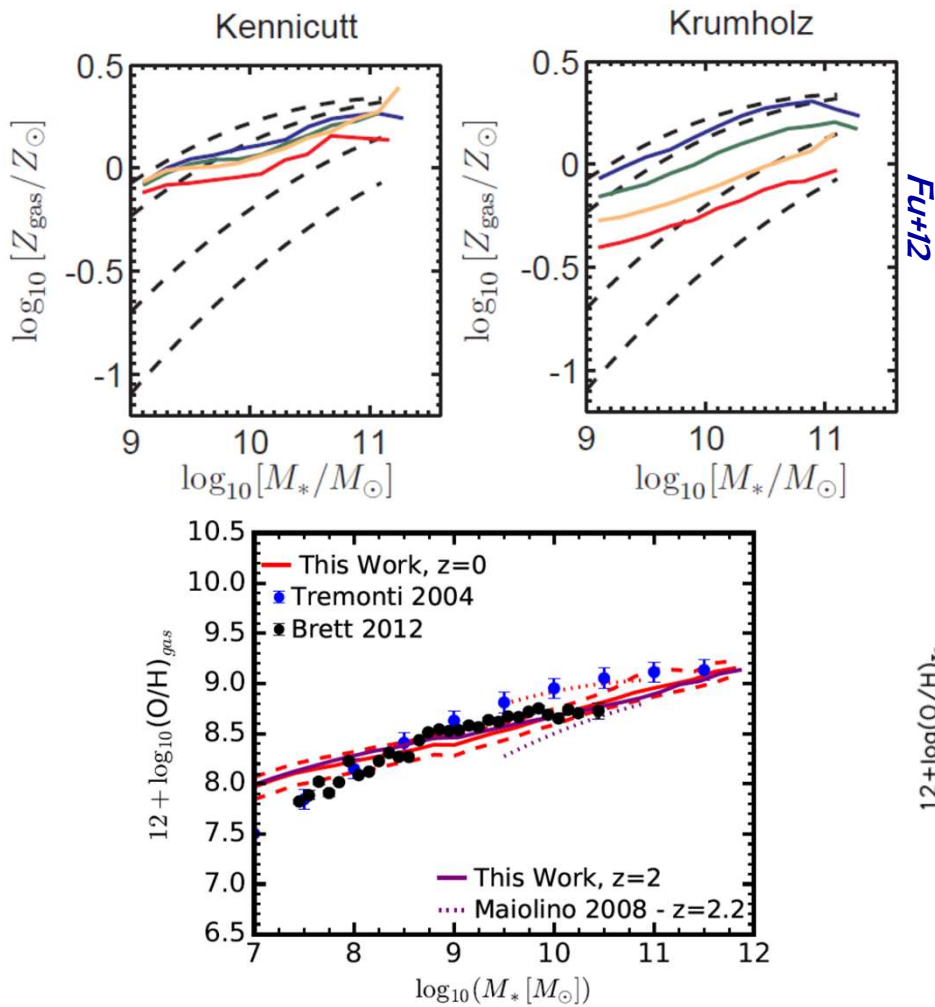
$M_{\star} - Z_g$ relation

Previously a good match to the $z=0$ MZ_gR

But what is the true MZ_gR ?

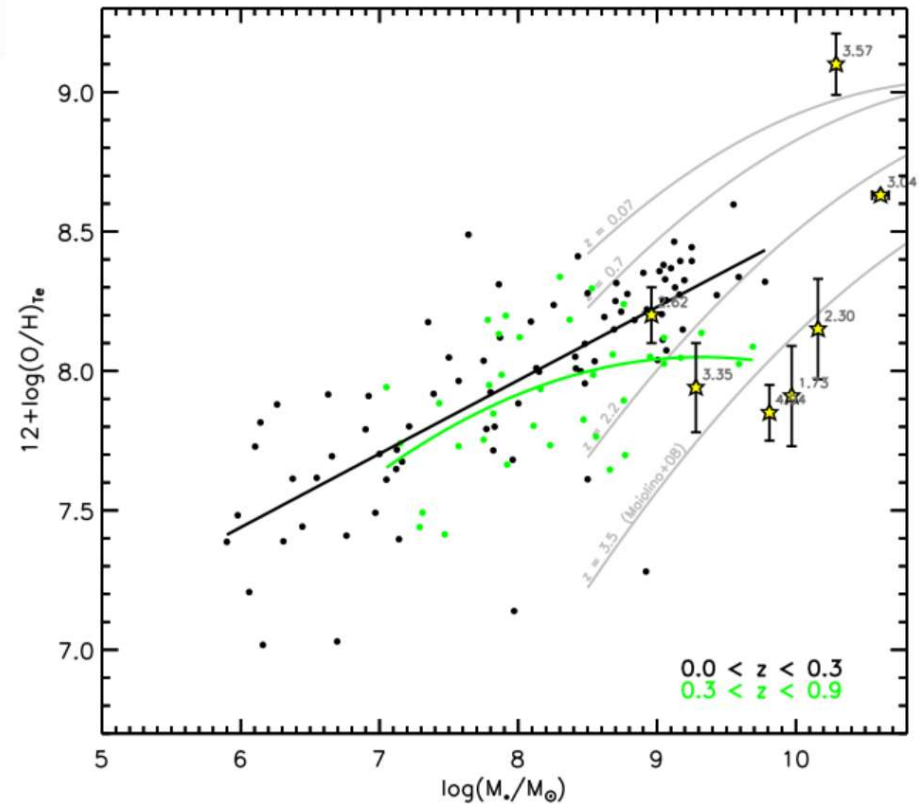


$M_\star - Z_g$ relation



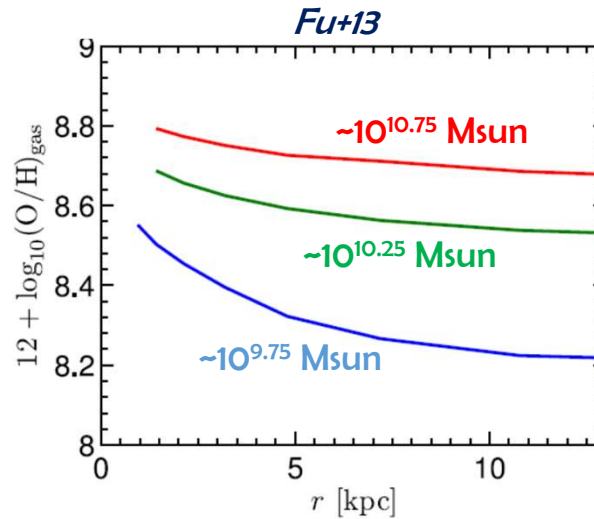
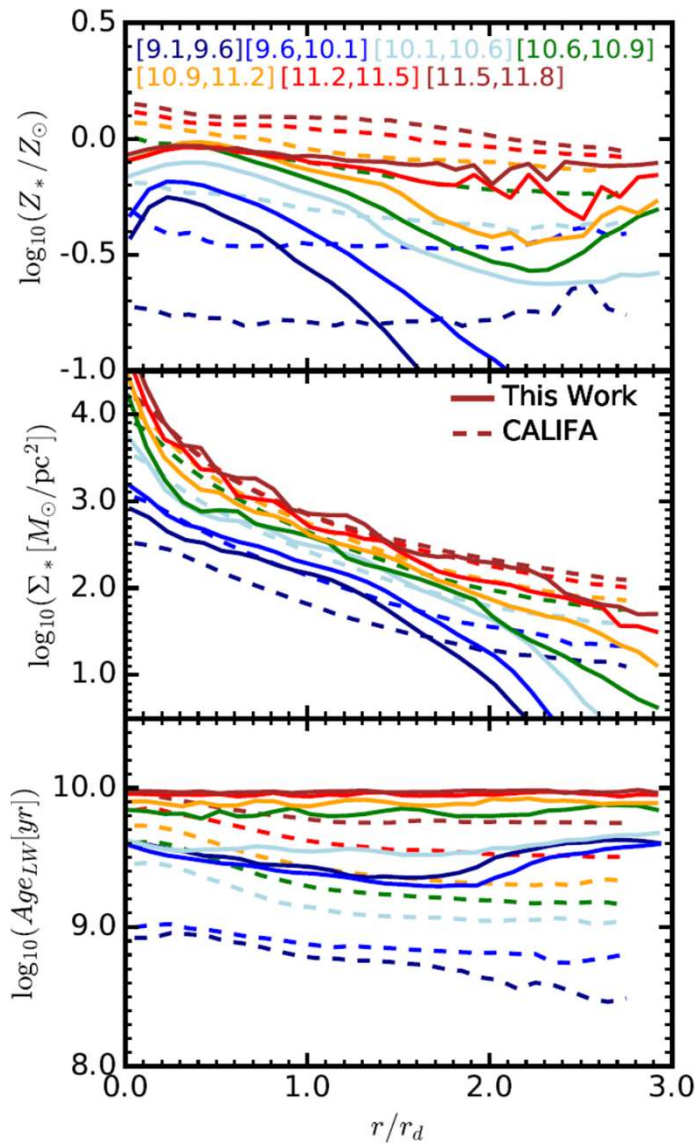
A large MZ_gR evolution is difficult for L-GALAXIES

Yates in prep.



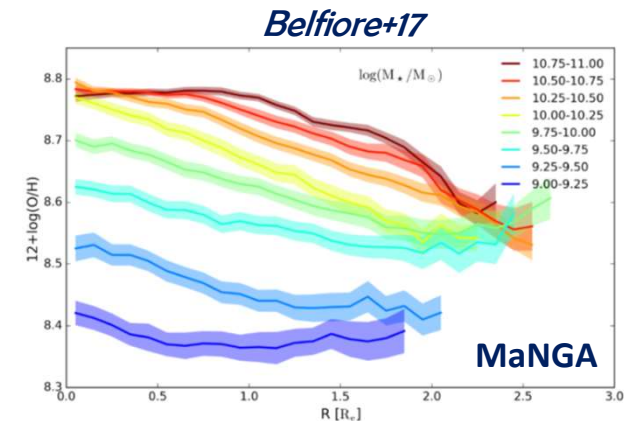
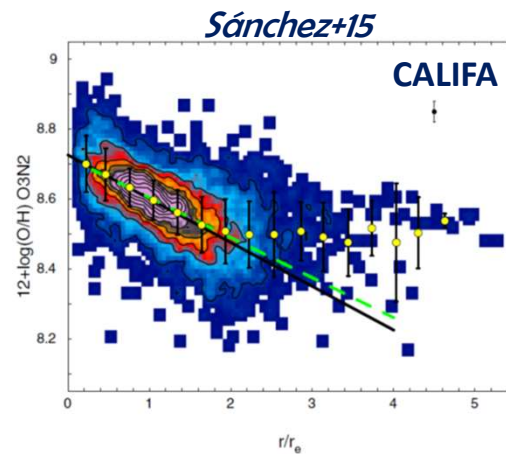
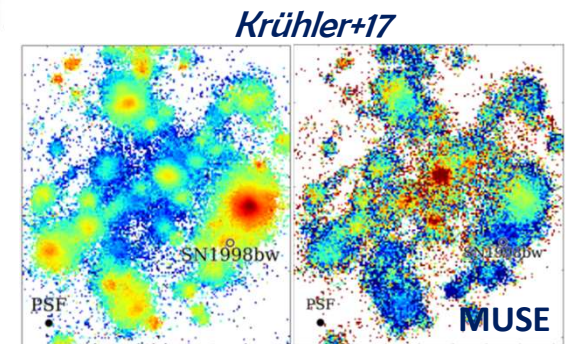
But how large is the true MZ_gR evolution anyway?...

Metallicity gradients



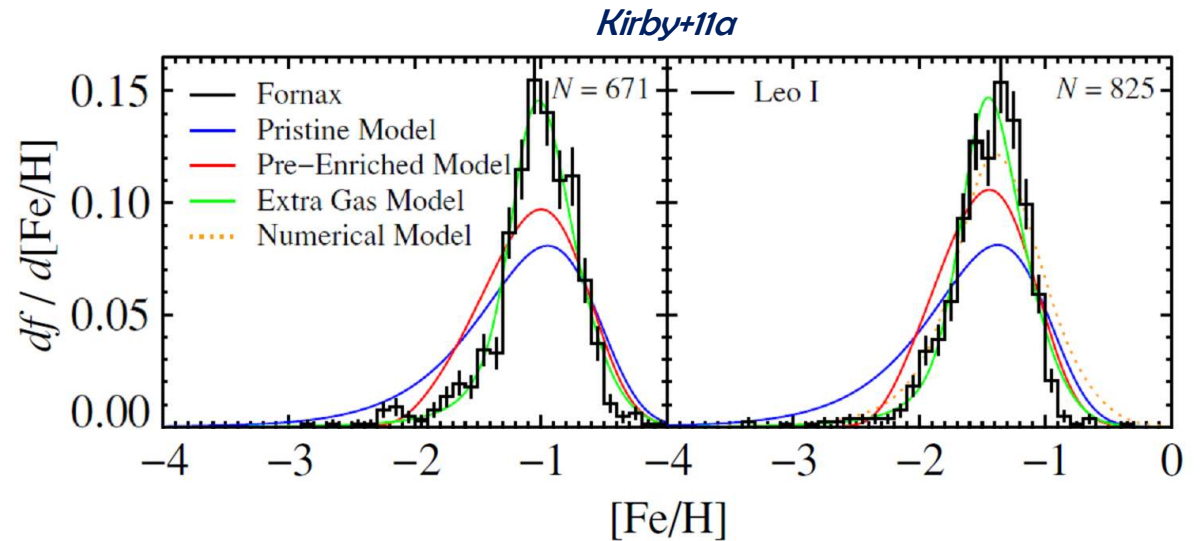
Metallicity gradients in the gas & stars are the next big step

But can we trust the latest observations?...



Dwarfs & bulges

Metallicity distributions in Local Group dwarfs:
(use ELUCID or *Caterpillar* haloes?)



Metallicity distributions in the MW bulge:
(multiple formation epochs and/or mechanisms?)

